



Article Configuration of the Deep Neural Network Hyperparameters for the Hypsometric Modeling of the *Guazuma crinita* Mart. in the Peruvian Amazon

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Abstract: The Guazuma crinita Mart. is a dominant species of great economic importance for the inhabitants of the Peruvian Amazon, standing out for its rapid growth and being harvested at an early age. Understanding its vertical growth is a challenge that researchers have continued to study using different hypsometric modeling techniques. Currently, machine learning techniques, especially artificial neural networks, have revolutionized modeling for forest management, obtaining more accurate predictions; it is because we understand that it is of the utmost importance to adapt, evaluate and apply these methods in this species for large areas. The objective of this study was to build and evaluate the efficiency of the use of a deep neural network for the prediction of the total height of Guazuma crinita Mart. from a large-scale continuous forest inventory. To do this, we explore different configurations of the hidden layer hyperparameters and define the variables according to the function HT = f(x) where HT is the total height as the output variable and x is the input variable(s). Under this criterion, we established three HT relationships: based on the diameter at breast height (DBH), (i) HT = f(DBH); based on DBH and Age, (ii) HT = f(DBH, Age) and based on DBH, Age and Agroclimatic variables, (iii) HT = f(DBH, Age, Agroclimatology), respectively. In total, 24 different configuration models were established for each function, concluding that the deep artificial neural network technique presents a satisfactory performance for the predictions of the total height of Guazuma crinita Mart. for modeling large areas, being the function based on DBH, Age and agroclimatic variables, with a performance validation of RMSE = 0.70, MAE = 0.50, bias% = -0.09and VAR = 0.49, showed better accuracy than the others.

Keywords: deep learning; artificial neural network; total height; forest management

1. Introduction

The *Guazuma crinita* Mart. (Bolaina Blanca) is characterized as a fast-growing forest species established in plantations in which it reaches growth maturity by the eighth or ninth year, being ready for harvesting [1,2]. The wood has a high commercial value and is used to obtain round and sawn wood for the manufacture of stretchers, boxes, laminates, toys, matches, handicrafts, plywood, construction and coating of houses and the obtaining of cellulose for paper, contributing to the livelihood of local farmers [3,4]. According to the Servicio Nacional Forestal y de Fauna Silvestre [5], there is 8530.76 ha of Bolaina Blanca plantations in Peru, which represents 503,839.71 m³ of standing trees.

A hypsometric model is generally expressed between the height and diameter relationship of a tree; however, it has also been shown that the variables of age, basal area, site



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). index, number of individuals per hectare, quadratic diameter, diameter and age classification, have influence with height [6,7]. It is very common to apply hypsometric modeling to reduce the costs and time of an inventory, as well as to contribute to the planning and forecasting of the volumetric production of plantations [8,9].

Deep learning is a type of automatic learning in which the same pattern of an artificial neural network (ANN) is followed, i.e., an architecture is defined and connections between them are shown [10]. ANNs often work with a single hidden quantity layer, but when used larger they are called deep neural networks (DNNs) or deep learning [11]. In other words, the big difference between ANN and DNN is that the latter model allows for multiple computations using processing layers to learn data representations with various levels of abstraction [11,12].

Hyperparameters are defined as parameters whose values control the learning process. A hyperparameter exploration is performed in order to test various configurations to obtain a better-performing model. This process is called hyperparameter optimization [13]. Such optimization can be done manually using empirical rules [14] or also with automated search [15], to reduce processing time and human effort, increasing productivity and throughput in scientific studies [16].

DNNs have been used to solve complex problems in the forestry and environmental area, such as identification of the origin of carbon through macroscopic images [17], to map Amazonian palm species at the individual tree crown level (ITC) using images RGB [18], species classification based on terrestrial laser scanning [19], for a rapid and efficient evaluation of forest damage after an environmental disaster [20]. It has even been shown in various studies related to forest management that the use of machine learning techniques is more accurate than mathematical regression techniques in their statistical performance [21–28].

The use of deep learning has not found studies for hypsometric modeling of this species, either in the Peruvian Amazon territory, this being the main problem when a base of its adequate configuration is not found to model the height. We consider it extremely important to understand the development of the DNN with hypsometric modeling, especially when large areas and a large amount of data from the continuous forest inventory of Bolaina Blanca are housed. Our hypothesis was that the configuration of the hyperparameters directly affects the statistical estimates in the hypsometric modeling of the Bolaina Blanca. The objective of this study was to evaluate the efficiency of using a deep learning neural network to predict the total height of *Guazuma crinita* Mart. from a large-scale continuous forest inventory, having specific objectives: (i) to configure and train the neural network and (ii) to evaluate the performance of the functions for total height prediction.

2. Material and Method

2.1. Study Area and Database

The *Guazuma crinita* Mart. forest plantations are located between parallels 9°22'0.32" and 9°41'52.60" S and meridians 74°51'03.18" and 75°02'33.18" W, between the districts of Puerto Inca and Yuyapichis, province of Puerto Inca, department of Huánuco, in the central Amazonian of Peru (Figure 1). The database comes from continuous forest inventory plots with measurements taken in the period 2009 to 2016. Data from 626 permanent measurement plots (PPM) were used, rectangular in shape randomly distributed with dimensions from 403 to 1509 m², with a total of 135,016 measurements equivalent to an area of 9834 hectares, with plot information: number, area, age, number of trees per plot, diameter at breast height measured at 1.3 m height (DBH) and total height (HT), measured with caliper and suunto hypsometer, respectively. Table 1 shows their descriptive statistics of dendrometric and agroclimatological variables.

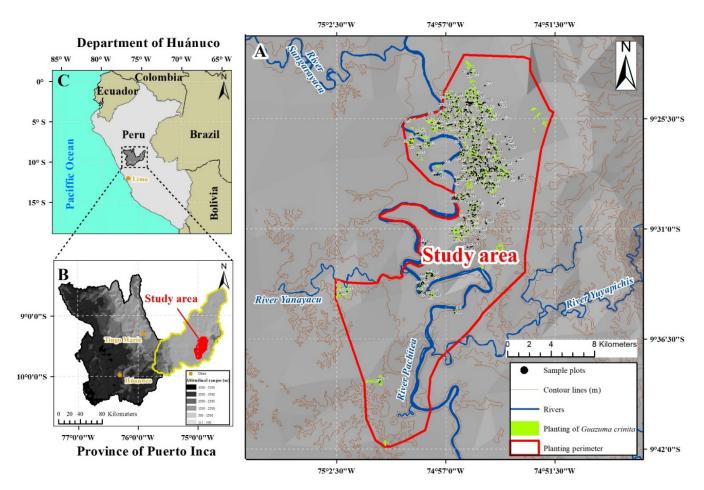


Figure 1. Location of the study and the forest plantations area of *Guazuma crinita* Mart. (**A**) in the Province of Puerto Inca (**B**), Department of Huánuco (**C**), Peruvian Amazon.

Table 1. Descriptive statistics of the dendrometric and agroclimatic variables of the <i>Guazuma crinita</i>
Mart. in the Peruvian Amazon.

	Descriptive Statistics										
Dendrometric	Mean	Minimum	Maximum	Variance	Std.Dev.	Coef.Var.					
Age (years)	2.56	0.40	7.30	1.63	1.28	49.92					
DBH (cm)	10.70	0.50	29.60	20.22	4.50	42.01					
HT (m)	11.05	3.00	25.82	22.63	4.76	43.03					
Agroclimatic											
Surface Pressure (kPa)	97.52	97.47	97.56	0.00	0.03	0.03					
Temperature at 2 Meters (°C)	26.98	26.40	28.47	0.45	0.67	2.49					
Specific Humidity at 2 Meters (g/kg)	16.08	15.01	17.15	0.47	0.68	4.25					
Relative Humidity at 2 Meters (%)	73.07	63.00	78.31	23.92	4.89	6.69					
Wind Speed at 2 Meters (m/s)	0.06	0.05	0.09	0.00	0.02	29.51					
Surface Soil Wetness	0.61	0.50	0.70	0.00	0.06	9.73					
Temperature at 2 Meters Maximum (°C)	39.10	38.09	39.73	0.45	0.67	1.71					
Temperature at 2 Meters Minimum (°C)	18.29	17.33	19.24	0.40	0.63	3.45					
Profile Soil Moisture	0.66	0.62	0.72	0.00	0.03	4.39					
Root Zone Soil Wetness	0.65	0.62	0.72	0.00	0.03	4.67					
Wind Speed at 2 Meters Maximum (m/s)	0.66	0.55	0.73	0.00	0.07	9.89					
Wind Speed at 10 Meters Maximum (m/s)	2.18	2.04	2.30	0.01	0.11	5.14					
Wind Speed at 10 Meters Minimum (m/s)	0.02	0.01	0.03	0.00	0.01	37.80					
Precipitation Corrected (mm/day)	3.01	1.75	4.37	0.57	0.76	25.12					
Wind Speed at 10 Meters Range (m/s)	2.16	2.01	2.27	0.01	0.11	5.02					
All Sky Surface UVA Irradiance (W/m ²)	11.71	11.40	12.03	0.05	0.22	1.89					
All Sky Surface UVB Irradiance (W/m ²)	0.35	0.34	0.36	0.00	0.01	2.65					
All Sky Surface Shortwave	4440										
DownwardIrradiance (MJ/m ² /day)	16.19	15.63	16.56	0.12	0.35	2.16					
Clear Sky Surface Shortwave											
DownwardIrradiance (MJ/m ² /day)	24.07	23.81	24.23	0.03	0.18	0.73					
All Sky Surface PAR Total (W/m^2)	87.58	84.65	89.74	3.28	1.81	2.07					
Clear Sky Surface PAR Total (W/m^2)	128.36	126.02	129.62	1.48	1.22	0.95					

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The plantations are distributed at altitudes that vary between 180 and 500 m above sea level, the average annual temperature is 27 °C, the average annual relative humidity is 85% and the annual precipitation varies between 2000 and 3000 mm, with greater intensity of precipitation between the months of November to March [29]. According to Holdridge [30] life zone classification, the study area is located in a region covered by tropical humid forest (bh-T), very humid tropical forest (bmh-T), and very humid transitional tropical forest (bmh-T).

In this study we used agroclimatic variables extracted from the NASA Prediction Of Worldwide Energy Resources website: https://power.larc.nasa.gov/ (accessed on 12 November 2021). Through the coordinates of each plot from 2009 to 2016, using the annual average in the predictions. The downloaded variables were: Surface Pressure (kPa), Temperature at 2 Meters (°C), Specific Humidity at 2 Meters (g/kg), Relative Humidity at 2 Meters (%), Wind Speed at 2 Meters (m/s), Surface Soil Wetness, Temperature at 2 Meters Maximum (°C), Temperature at 2 Meters Minimum (°C), Profile Soil Moisture, Root Zone Soil Wetness, Wind Speed at 2 Meters Maximum (m/s), Wind Speed at 10 Meters Minimum (m/s), Precipitation Corrected (mm/day), Wind Speed at 10 Meters Range (m/s), All Sky Surface UVA Irradiance (W/m²), All Sky Surface UVB Irradiance (MJ/m²/day), Clear Sky Surface Shortwave Downward Irradiance (MJ/m²/day), All Sky Surface PAR Total (W/m²).

2.2. Variable Input, Output, and Data Splitting in Training and Validation

For model fitting, we used the technique of deep artificial neural networks using the H20 pack [31] in R [32]. We set the function HT = f(x), where HT is the output variable and x is the input variable(s). Under this criterion, we established three HTrelationships: depending on the DBH variable, (i) HT = f(DBH); based on DBH and Age, (ii) HT = f(DBH, Age) and based on DBH, Age and agroclimatic variables, (iii) HT = f(DBH,Age, Agroclimatology), respectively. All downloaded agroclimatic variables were included in the third function. These functions were trained separately, they were configured with different hyperparameters and their performance was compared. In total, we performed 72 training runs, i.e., 24 training models for each HT = f(x) function set in this study.

The data was standardized and randomly separated establishing 70% of the data for Training and 30% for Validation.

2.3. Hyper-Parameter Tuning

2.3.1. Layers, Units, and Activation Function

Their architectures had one input layer, two, three, and five hidden layers and one output layer. The numbers of neurons or units in the hidden layer were 10:10 (Figure 2A), 10:5 (Figure 2B), 10:5:2 (Figure 2C), 50:50 (Figure 2D), 50:25 (Figure 2E), 50:25:5 (Figure 2F), 10: 5:2:5:10 (Figure 2G), and 50:25:5:25:50 (Figure 2H).

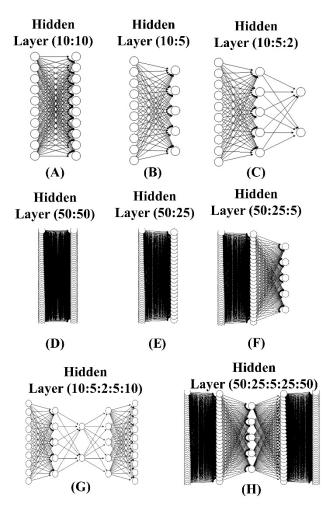


Figure 2. Number of neurons or units in the hidden layer used for hypsometric modeling of the *Guazuma crinita* Mart. in the Peruvian Amazon. The numbers of neurons in the hidden layer were 10:10 (**A**), 10:5 (**B**), 10:5:2 (**C**), 50:50 (**D**), 50:25 (**E**), 50:25:5 (**F**), 10: 52:5:10 (**G**), and 50:25:5:25:50 (**H**).

The Tanh (Equation (1)), Rectified Linear (Equation (2)), and Maxout (Equation (3)) activation functions were used in the hidden layer, while in the output layer we use the Linear (Equation (4)) activation function for all cases.

$$f(\alpha) = \frac{e^{\alpha} - e^{-\alpha}}{e^{\alpha} + e^{-\alpha}}; f(.) \in [-1, 1]$$
(1)

$$f(\alpha) = \max(0, \alpha); f(.) \in \mathbb{R}_+$$
(2)

$$f(.) = \max(w_i x_i + b); f(.) \in [-\infty, 1]; \text{ rescale if } \max f(.) \ge 1$$
(3)

$$f(\alpha) = \alpha \tag{4}$$

where *f* is the function that represents the non-linear activation used in the entire neural network, *b* is the bias for the neuron activation threshold, x_i and w_i denote the input values of the unit or neuron and their weights; α denotes the weighted combination:

$$\alpha = \sum_{j=1}^n w_i x_i + b.$$

2.3.2. Distribution and Loss Functions

The Gaussian distribution function was specified as equivalent to wMSE (weighted mean squared error) (Equation (5)) as it was, our numerical response variable and the loss function chosen was quadratic (Equation (6)):

$$f(.) = \omega (y - f)^2 \tag{5}$$

where *y* is a true response, *f* is a predicted response, and ω is weighted.

$$L(W, B | j) = \frac{1}{2} | ||t^{(j)} - o^{(j)}||_2^2$$
(6)

where $t^{(j)}$ and $o^{(j)}$ are the predicted and actual output; j and W is the collection $\{W_i\}_{1:N-1}$: W_i denotes the weight matrix connecting layers i and i + 1 for a network of N layers; B is the collection $\{b_i\}_{1:N-1}$: b_i denotes the column vector of biases for layer i + 1.

2.3.3. Optimization Algorithm, Regularization, Epoch, and Batch Size

The optimization algorithm used in this study was the adaptive learning rate ADADELTA (Equation (7)) [33]. The mini-batch was of size 1, the number of epochs was 300, and the type of regularization was with the early stop system, with 5 stop rounds, stop tolerance of 0.001, and MSE (mean square error) stop metric.

$$E[g^{2}]_{t} = \rho E[g^{2}]_{t-1} + (1-\rho)g_{t}^{2}; \text{ Accumulate Gradient} \Delta\theta_{t} = -\frac{RMS[\Delta\theta]_{t-1}}{RMS[g]_{t}}g_{t}; \text{ Compute Update} E[\Delta\theta^{2}]_{t} = \rho E[\Delta\theta^{2}]_{t-1} + (1-\rho)\Delta\theta_{t}^{2}; \text{ Accumulate Updates}$$
$$\theta_{t+1} = \theta_{t} + \Delta\theta_{t}; \text{ Apply Update}$$
$$(7)$$

where θ_t denoting the parameters at the t-th iteration, g_t is the compute gradient, t is the time and RMS is the root mean squared error. For our study, the learning rate time decay factor (rho) was 0.99 and the learning rate time smoothing factor (epsilon) was 1×10^{-8} .

2.4. Model Performance

The estimates were analyzed according to [8,34]. The estimates of the training and testing data were with the statistical variables of Root Mean Squared Error, *RMSE* (Equation (8)), and Mean Absolute Error, *MAE* (Equation (9)). For testing data, we increased bias% (Equation (10)) and the variance error, *VAR* (Equation (11)). Likewise, percentage graphs of cases by percentage relative error, RE% (Equation (12)) were also interpreted. Figure 3 shows the methodological flowchart used in this study.

$$RMSE = \sqrt{n^{-1} \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2}$$
(8)

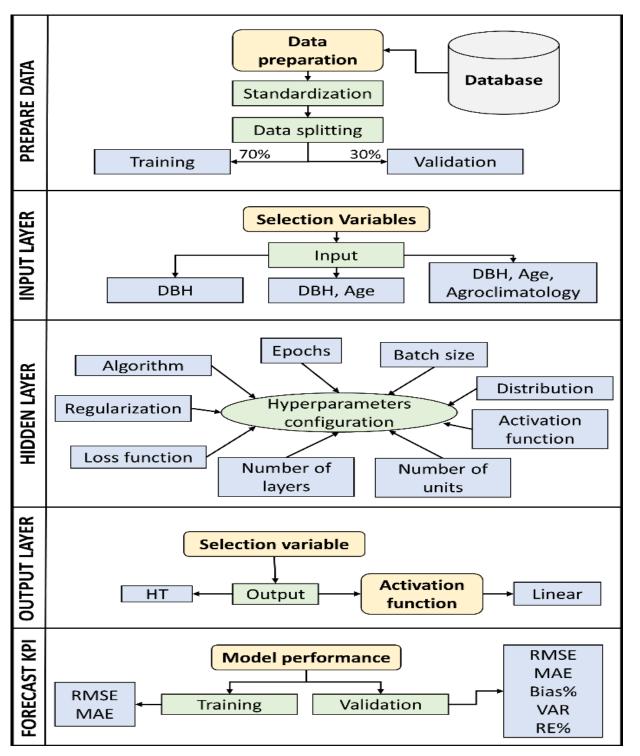
$$MAE = \left(n^{-1} \sum_{i=1}^{n} |Y_i - \hat{Y}_i| \right)$$
(9)

$$Bias\% = \frac{Bias}{\overline{Y}} \times 100; \ Bias = \frac{\sum_{i=1}^{n} Y_i - \hat{Y}_i}{n}$$
(10)

n

$$VAR = \frac{\sum \left(bias - (Y_i - \hat{Y}_i)\right)^2}{n - 1} \tag{11}$$

$$RE\% = \frac{Y_i - \hat{Y}_i}{Y} \times 100 \tag{12}$$



where *n* = the number of observations for the measurer, Y_i = observed total height value_i, \hat{Y}_i = predicted total height value_i, and \overline{Y} = mean of observed total height value_i.

Figure 3. Methodological flow diagram established in our study for the hypsometric modeling of *Guazuma crinita* Mart. trees in the Peruvian Amazon.

The data were processed with the following computer features:

- Operating System: Windows 10 Pro 64-bit
- CPU: Intel Core i3 6006U @ 2.00 GHz- Skylake-U/Y 14 nm Technology
- RAM: 12.00 GB Dual-Channel Unknown @ 1064MHz (15-15-15-35)
- Motherboard: LENOVO LNVNB161216 (U3E1)
- Graphics: Generic PnP Monitor (1366 \times 768@64 Hz)
- Storage: 465 GB Western Digital WDC WDS500G2B0B-00YS70 (SATA (SSD).

3. Results

3.1. Training Status

The maximum processing time for each model was 50 s. In Table 2 we can observe the status and architecture of each trained model according to each function. The trained models it was not necessary to complete the complete training epochs (300 epoch).

Table 2. State and architecture of each model trained according to the three functions evaluated for the predictions of the total height of the *Guazuma crinita* Mart. trees in the Peruvian Amazon.

Model	Hidde	en Layer	Epochs/Train			
	Activation Functions	Layers/Units	HT = f(DBH)	HT = f(DBH, Age)	HT = <i>f</i> (DBH, Age, Agroclimatology)	Total Layers
Model 1	Tanh	2(10:10)	34.9/3,300,864/151	35/3,307,955/161	17.4/1,647,234/371	4
Model 2	Rectifier	2(10:10)	89.9/8,496,703/151	60.3/5,700,023/161	30/2,835,773/371	4
Model 3	Maxout	2(10:10)	65/6,145,912/291	41/3,872,041/311	25.1/2,369,990/731	4
Model 4	Tanh	2(10:5)	64.5/6,100,250/91	48.7/4,599,721/101	17.1/1,614,741/311	4
Model 5	Rectifier	2(10:5)	195.7/18,497,950/91	159.8/15,100,404/101	30.4/2,869,197/311	4
Model 6	Maxout	2(10:5)	51.7/4,882,319/176	62.4/5,897,233/196	25/2,358,105/616	4
Model 7	Tanh	3(10:5:2)	70.9/6,698,582/100	73/6,901,805/110	32.9/3,108,612/320	5
Model 8	Rectifier	3(10:5:2)	92.1/8,702,945/100	148.1/14,000,065/110	30.6/2,892,184/320	5
Model 9	Maxout	3(10:5:2)	85.7/8,097,387/197	77/7281,256/217	21.7/2,051,691/637	5
Model 10	Tanh	2(50:50)	5.4/509,363/2751	6.7/637,904/2801	7.9/744,223/3851	4
Model 11	Rectifier	2(50:50)	44.5/4,207,558/2751	27.7/2,615,333/2801	11.6/1,093,767/3851	4
Model 12	Maxout	2(50:50)	10.7/1,007,812/5451	10.7/1,008,106/5551	10.8/1,023,225/7651	4
Model 13	Tanh	2(50:25)	9.7/917,479/1451	13.2/1,251,731/1501	5.7/542,308/2551	4
Model 14	Rectifier	2(50:25)	37.5/3,547,655/1451	23.9/2,260,683/1501	12/1,132,858/2551	4
Model 15	Maxout	2(50:25)	13/1,230,927/2876	9.4/885,209/2976	11/1,035,577/5076	4
Model 16	Tanh	3(50:25:5)	7.9/748,206/1561	8.9/843,398/1611	8.3/783,786/2661	5
Model 17	Rectifier	3(50:25:5)	41.7/3,939,088/1561	23.6/2,226,682/1611	20/1,893,917/2661	5
Model 18	Maxout	3(50:25:5)	23.4/2,215,252/3116	9.6/907,092/3216	9.1/857,062/5316	5
Model 19	Tanh	5(10:5:2:5:10)	54/5,103,702/183	53/5,009,328/193	44.4/4,197,664/403	7
Model 20	Rectifier	5(10:5:2:5:10)	160.8/15,202,054/183	65.6/6,200,261/193	39.6/3,738,971/403	7
Model 21	Maxout	5(10:5:2:5:10)	42.3/4,001,607/355	35.2/3,328,508/375	23.7/2,240,775/795	7
Model 22	Tanh	5(50:25:5:25:50)	10.1/955,656/3056	8/760,293/3106	6.3/598,638/4156	7
Model 23	Rectifier	5(50:25:5:25:50)	29.3/2,766,703/3056	35.7/3,369,835/3106	12.3/1,160,523/4156	7
Model 24	Maxout	5(50:25:5:25:50)	11.3/1,072,656/6061	13.9/1,309,262/6161	10.5/996,059/8261	7

The networks trained from the HT = f(DBH) function obtained between 5.4 and 195.7 training epochs, 509,363 and 1,8497,950 training samples, 91 and 6061 weights and bias. The HT = f(DBH, Age) function was obtained between 6.7 and 158.9 training epochs, 637,904 and 15,100,404 training samples, 101 and 6161 weights and biases. The HT = f(DBH, Age, Agroclimatology) function was obtained between 5.7 and 44.4 training times, 542,308 and 4,197,664 training samples, 311 and 8261 weights and biases.

Complete training status of each model and type of function evaluated used to predict the total height of *Guazuma crinita* Mart. in the Peruvian Amazon, it can be seen in Table S1.

3.2. Model Validation Performance

We statistically analyzed each trained model with its respective function, evaluating the performance of RMSE, MAE for training, and we increased two more parameters for validation (Table 3). In general, all models with their responsive function showing a good performance. The HT = f(DBH) function showed a result that varies $1.26 \le RMSE \le 2.07$

and $0.93 \leq MAE \leq 1.79$ for training and $1.26 \leq RMSE \leq 2.06$, $0.93 \leq MAE \leq 1.78$, $-1.84 \leq Bias\% \leq 10.95$ and $1.44 \leq VAR \leq 2.78$ for validation. The function HT = f(DBH, Age) showed a result that varies $0.70 \leq RMSE \leq 0.78$ and $0.49 \leq MAE \leq 0.57$ for training and $0.71 \leq RMSE \leq 0.78$, $0.49 \leq MAE \leq 0.57$, $-1.24 \leq Bias\% \leq 2.32$, $0.49 \leq VAR \leq 0.60$ for validation. The function HT = f(DBH, Age, Agroclimatology) showed a result that varies $0.70 \leq RMSE \leq 0.79$ and $0.50 \leq MAE \leq 0.54$ for training and $0.70 \leq RMSE \leq 0.79$, $0.50 \leq MAE \leq 0.55$, $-0.23 \leq Bias\% \leq 2.27$ and $0.48 \leq VAR \leq 0.57$ for validation.

Table 3. Performance of the statistics of each model trained and function evaluated, both for training and for validation in the total height predictions of the *Guazuma crinita* Mart. in the Peruvian Amazon.

HT = f(DBH)						HT = f(DBH, Age)						HT = f(DBH, Age, Agroclimatology)						
	Train Validation					Train Validation					Tra	in		Validation				
Model	RMSE	MAE	RMSE	MAE	Bias%	VAR	RMSE	MAE	RMSE	MAE	Bias%	VAR	RMSE	MAE	RMSE	MAE	Bias%	VAR
Model 1	1.42	1.19	1.43	1.2	6.04	1.61	0.78	0.57	0.77	0.57	-0.63	0.6	0.76	0.52	0.76	0.52	1.67	0.54
Model 2	1.46	1.23	1.47	1.24	6.32	1.67	0.76	0.53	0.75	0.52	0.84	0.55	0.76	0.52	0.76	0.52	1.11	0.56
Model 3	1.38	1.13	1.4	1.14	4.65	1.68	0.75	0.52	0.74	0.51	1.18	0.53	0.76	0.53	0.76	0.53	2.23	0.51
Model 4	1.42	1.17	1.44	1.19	4.5	1.82	0.74	0.51	0.73	0.51	0.24	0.54	0.75	0.52	0.76	0.52	1.52	0.55
Model 5	1.39	1.14	1.41	1.16	5.74	1.58	0.78	0.54	0.77	0.53	2.02	0.55	0.77	0.53	0.76	0.53	0.85	0.57
Model 6	1.4	1.15	1.42	1.17	5.38	1.66	0.77	0.54	0.76	0.53	2.32	0.52	0.77	0.54	0.76	0.54	1.99	0.54
Model 7	1.32	1.05	1.32	1.06	2.78	1.66	0.75	0.51	0.75	0.51	1.49	0.54	0.73	0.51	0.74	0.51	1.3	0.52
Model 8	1.38	1.12	1.39	1.13	4.81	1.64	0.72	0.5	0.71	0.5	1.02	0.5	0.78	0.54	0.77	0.54	1.44	0.56
Model 9	1.4	1.15	1.43	1.17	5.43	1.67	0.75	0.53	0.75	0.52	1.85	0.52	0.73	0.51	0.74	0.51	1.02	0.53
Model 10	1.29	1.04	1.29	1.04	3.38	1.54	0.73	0.53	0.73	0.53	1.52	0.5	0.74	0.52	0.74	0.52	1.52	0.52
Model 11	1.43	1.19	1.44	1.19	5.43	1.71	0.73	0.5	0.74	0.51	1.21	0.52	0.75	0.54	0.75	0.53	2.06	0.51
Model 12	1.32	1.1	1.33	1.11	5.08	1.46	0.72	0.52	0.71	0.51	0.58	0.5	0.73	0.53	0.73	0.53	1.05	0.52
Model 13	1.31	1.04	1.33	1.05	2.96	1.66	0.72	0.51	0.72	0.51	1.07	0.51	0.79	0.54	0.77	0.54	2.27	0.54
Model 14	1.34	1.09	1.36	1.1	4.45	1.61	0.74	0.52	0.75	0.53	0.46	0.55	0.78	0.54	0.79	0.54	2.03	0.57
Model 15	1.39	1.14	1.39	1.13	5.43	1.56	0.72	0.51	0.72	0.51	1.67	0.49	0.7	0.5	0.7	0.5	-0.09	0.49
Model 16	1.28	1.04	1.29	1.04	2.63	1.58	0.72	0.52	0.72	0.51	0.7	0.51	0.72	0.5	0.73	0.5	1.05	0.52
Model 17	1.41	1.15	1.42	1.15	5.24	1.68	0.77	0.52	0.78	0.53	1.87	0.56	0.78	0.54	0.79	0.55	2.05	0.57
Model 18	1.31	1.08	1.34	1.1	5.32	1.44	0.73	0.55	0.74	0.55	1.06	0.53	0.75	0.52	0.75	0.52	1.04	0.54
Model 19	2.07	1.79	2.06	1.78	10.95	2.78	0.75	0.53	0.75	0.53	0.52	0.56	0.74	0.52	0.73	0.51	0.31	0.53
Model 20	1.31	1.04	1.33	1.04	3.2	1.63	0.74	0.53	0.74	0.52	0.61	0.54	0.75	0.52	0.73	0.51	0.83	0.53
Model 21	1.44	1.21	1.43	1.2	5.63	1.67	0.77	0.57	0.77	0.57	-1.24	0.57	0.73	0.52	0.72	0.52	1.18	0.51
Model 22	1.28	0.96	1.28	0.95	-0.04	1.63	0.7	0.5	0.71	0.5	0.61	0.5	0.74	0.52	0.74	0.51	0.78	0.54
Model 23	1.41	1.13	1.4	1.12	4.9	1.67	0.72	0.49	0.72	0.49	1.25	0.5	0.73	0.52	0.72	0.52	-0.23	0.52
Model 24	1.26	0.93	1.26	0.93	-1.84	1.55	0.76	0.52	0.74	0.52	2.03	0.5	0.72	0.5	0.72	0.5	1.73	0.48

To recognize the model of each function, we not only analyze the forecast Key Performance Indicator (KPI). We also analyze the residual plot; that is, the relative error in percentage between the predicted values (Figure 4) and the bias-variance tradeoff (Figure 5). According to the results, model 24 of the function HT = f(DBH) with RMSE = 1.26 and MAE = 0.93, model 12 of the function HT = f(DBH, Age) RMSE = 0.71 and MAE = 0.51, and model 15 of the function HT = f(DBH, Age, Agroclimatology) RMSE = 0.70 and MAE = 0.50, present a better performance than the others.

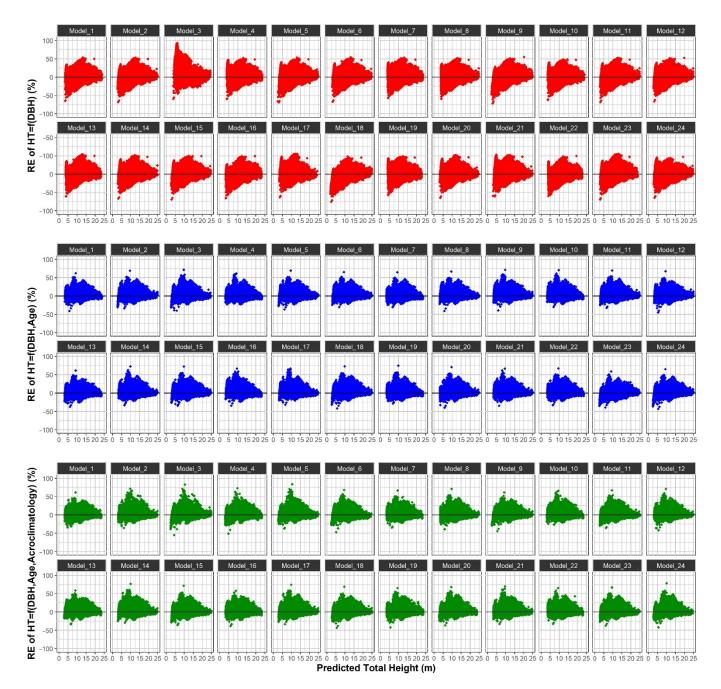


Figure 4. Residual graph in relation to the predicted total height for the hypsometric modeling of the trees of *Guazuma crinita* Mart. in the Peruvian Amazon, for each trained model and based on the three study functions: HT = f(DBH), HT = f(DBH, Age) and HT = f(DBH, Age, Agroclimatology).

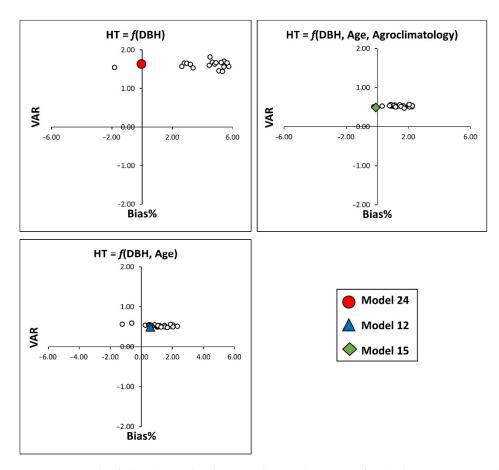


Figure 5. Graph of the relationship between bias and variance for the hypsometric modeling of *Guazuma crinite* Mart. trees in the Peruvian Amazon, showing with greater emphasis the best trained model for each of the three study functions: HT = f(DBH), HT = f(DBH, Age) and HT = f(DBH, Age), Agroclimatology).

4. Discussion

4.1. Training Status for the Prediction of the Total Height of Bolaina Blanca

All the trained models did not need to complete the 300 number of epochs to converge the weights, because thanks to the regularization of early stopping the training of the models stopped as they did not present improvements in the validation metric, this method is not very intrusive and minimizes established metric across epochs [35], however stopping too early can enlarge bias and reduce variance, just as stopping too late can reduce bias and enlarge variance [36], that is why the importance of performing a hyperparameter optimization search with several trainings and observing the variance and bias compensation, adapting it for each type of problem [37]. In our study, model 5 of the HT = f(DBH)function needed the greatest number of epochs to converge the weights, with 195.7 epochs, and model 10 of the HT = f(DBH) function needed the least amount of epochs. to converge the weights with 5.4 epochs, which leads to a greater and lesser process of training time, respectively. However, model 24 of the function HT = f(DBH), model 12 of the function HT = f(DBH, Age) and model 15 of the function HT = f(DBH, Age, Agroclimatology)with 11.3, 10.7 and 11 number of epochs, respectively, present a better performance in their statistical evaluations than the rest (Table 3). Regarding its typology of number of neurons, the best networks of each function were 2 (50:50), 5 (50:25:5:25:50), and 2 (50:50), respectively, this is relatively dependent on In each study, in case of presenting too much information, more neurons will be needed to converge the weights [38] and more hidden layers in the model will be more complex or deep. The hidden layer activation function of the best performing models was maxout, the advantage of this hidden layer activation function is that the network learns the relationship between the hidden units and also the

activation function of each hidden unit [35] but doubles the number of parameters for each neuron, which leads to a high total number of parameters [11], as shown in Table 2, the increase in the weights of the training used. This maxout function was initially presented as a natural companion using dropout to train convolutional networks, but studies have also been carried out without dropout as a substitute for the sigmoidal function and it has even been tested to solve regression problems, producing good results [39]. Although it is true, until the completion of this manuscript, that deep learning techniques have not been used for Bolaina Blanca tree height predictions, many studies have been conducted in other species using classical artificial neural network (ANN) techniques in other species, i.e., with a single hidden layer, in a large part of all these studies have been used with sigmoidal activation function, such as the hyperbolic and sigmoid tangent, obtaining satisfactory results [7,40–42]. The processing time of the modeling functions depends on the characteristics of the computer and is relative, however, the execution of our configurations for the height mode does not require a high demand on the characteristics of the computer from the user.

4.2. Growth and Estimation of the Total Height of Bolaina Blanca

In Peru, forestry and forest management of the species of *Guazuma crinita* Mart. It has been extensively studied since 1992 by Vidaurre and Héctor [43], evaluating its growth and the optimal sites for the development of the species. Subsequently, its economic importance is studied [44], becoming the dominant species for the sustenance of farmers in the Peruvian Amazon, initially opening up to a series of investigations, such as its geographical variation in its growth and wood density [45], modeling of its production [46]. However, it was not until 2018 that the total height of the species was modeled for the first time by Elera Gonzáles [47] in the Peruvian Amazon, in which she used regression techniques applying six hypsometric models, obtaining as a result of the performance of the models a range of $1.86 \le \text{RMSE} \le 1.93$ and $1.44 \le \text{MAE} \le 1.52$, it should be noted that these hypsometric models had a relationship of total height between DBH, DBH dominant and Age. In our study using a DNN, it exceeds the statistical performances (Table 3) and it is very likely that it also exceeds when ANN techniques are used, for smaller areas. When we analyzed the best configurations obtained in our study, the relationship between height and diameter, HT = f(DBH), the RMSE result was 1.26 (Model 24). The performance increases when we increase the relation between the DBH and age, HT = f(DBH, Age) with RMSE = 0.71 (Model 12) and even more when it is related to agroclimatic variables, HT = f(DBH, Age, Agroclimatology), with RMSE = 0.70 (Model 15). As we can see, obtaining a relationship between diameter and height in this species is relatively complex using regression techniques, and could even worsen if biased data were used, especially from inventories of plantation areas that have not received uniform forest management. The inclusion of climatological variables could bias the modeling for the prediction of the total height of the species (Figure 5), these directly influence decisionmaking for forest planning, such as silvicultural treatments, land acquisition, and genotype selection [48], in which various studies have shown better performance using agroclimatic variables, especially for growth and production models in eucalyptus plantations [49–52].

The models used in this study are efficient, both statistically and practically, as we highlight a specific configuration for each function used. We developed three functions to be adapted to different areas of the Peruvian Amazon, according to the database of each community. As the first function, we use only the diameter as an independent variable, being able to be considered as a guide for local communities with smaller-scale production, where plantations are not monitored (age or other variables of the forest mass). The second and third functions are for companies or cooperatives with medium or large-scale plantations, where permanent monitoring is carried out.

Extrapolation beyond the levels of the predictor variables, for example, dbh, will always have some risk, so the application to values outside the ranges observed in the study requires caution on the part of the reader in the application of the functions. However, although it may be a limitation, the range observed in the data covers a very large range of occurrences of values in the predictor variables, resulting in a great potential for the use of the proposed models. The study is a great contribution to the scientific community, farmers, and companies dedicated to the modeling and production of *Guazuma crinita* Mart. in the Peruvian Amazon.

5. Conclusions

The deep artificial neural network technique presents satisfactory performance for predictions of the total height of *Guazuma crinite* Mart. in modeling large areas. In general, all the variables used to influence the predictions. However, the addition of the agroclimatic variables together with the diameter at breast height and age have shown better accuracy than the others. Our hyperparameter configuration proposal (Model 24—HT = f(DBH), Model 12—HT = f(DBH, Age) and Model 15—HT = f(DBH, Age, Agroclimatology)) present the best performance and can be adapted to other forest management problems using a large amount of data. Likewise, we recommend carrying out studies with data from pre-cut inventories and with the addition of categorical variables.

Supplementary Materials: The following are available online at https://www.mdpi.com/article/10.339 0/f13050697/s1, Table S1: Training status of each model and type of function evaluated used to predict the total height of *Guazuma crinita* Mart. in Peruvian amazon.

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